

Kloomock and Muffley,<sup>[2]</sup> and Raven.<sup>[3]</sup> We will follow Kloomock and Muffley's presentation here. Figure 7-8 shows two positions of the follower arm  $BC$  being rotated around a "stationary" cam in the typical inversion of the motion for analysis purposes. (Typically, the follower arm pivot  $B$  remains stationary and the cam rotates.) The initial position  $BC$  becomes  $B'C'$  at a later time after the cam has rotated through the angle  $\gamma$ . Though these positions are shown widely separated for clarity, the analysis considers them to be an infinitesimal angle  $d\gamma$  apart.

The pressure angle  $\phi$  is defined as the angle between the normal force  $N$  applied at the cam-roller interface, shown as vector  $C'N$ , and the direction of the velocity of the roller center, shown as  $C'D'$ . Neglecting friction and taking moments about the arm pivot  $B'$  gives

$$\frac{Nl}{T} = \frac{1}{\cos \phi} \quad (7.6)$$

where  $l$  is the length of the arm and  $T$  is the applied load torque on the follower arm. The torque ratio  $Nl/T$  is similar to the force magnification factor  $N/F$  of equation 7.1b for a radial cam with translating roller follower.

From the geometry of Figure 7-8, note that as  $d\gamma$  approaches zero,  $\gamma'$  approaches  $\gamma$ ,  $\delta'$  approaches  $\delta$ , and  $\varepsilon'$  approaches  $\varepsilon$ . An expression for pressure angle  $\phi$  can be written as:

$$\phi = \frac{\pi}{2} - (\varepsilon - \lambda) \quad (7.7a)$$

$$\lambda = \tan^{-1} \frac{1}{R} \frac{dR}{d\gamma} \quad (7.7b)$$

The triangle  $OB'C'$  in Figure 7-8a (and shown separately in Figure 7-8b) can be solved for  $R$ ,  $\varepsilon$ , and  $\psi$ .

$$R = \sqrt{l^2 + c^2 - 2lc \cos \delta} \quad (7.7c)$$

$$\varepsilon = \sin^{-1} \left( \frac{c}{R} \sin \delta \right) \quad (7.7d)$$

$$\psi = \cos^{-1} \left( \frac{c^2 + R^2 - l^2}{2Rc} \right) \quad (7.7e)$$

Also from Figure 7-8 it can be seen that

$$\gamma = \psi_0 - \psi + \theta \quad (7.7f)$$

Differentiating equation 7.7f with respect to  $R$ :

$$\frac{d\gamma}{dR} = \frac{d\theta}{dR} - \frac{d\psi}{dR} \quad (7.7g)$$

Differentiating equation 7.7c with respect to  $\theta$  and reciprocating: